



Semester Two Examination, 2018

Question/Answer booklet

**MATHEMATICS
APPLICATIONS
UNITS 1 AND 2
Section One:
Calculator-free**

SOLUTIONS

Student number: In figures

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In words

Your name

Time allowed for this section

Reading time before commencing work: five minutes

Working time: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Section One: Calculator-free**35% (52 Marks)**

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

Question 1**(5 marks)**

- (a) Solve the equation $4(5 - 2x) = x - 7$ for x .

(2 marks)

Solution
$20 - 8x = x - 7$
$27 = 9x$
$x = 3$
Specific behaviours
✓ expands LHS ✓ collects like terms and solves

- (b) Ash, Billie and Chris collected a total of 160 cans to recycle. Ash collected twice as many cans as Chris, Chris collected 12 more cans than Billie and Billie collected x cans.

Determine how many cans Billie collected.

(3 marks)

Solution
$x + (x + 12) + 2(x + 12) = 160$
$4x + 36 = 160$
$4x = 124$
$x = \text{Billie's cans} = 31$
Specific behaviours
✓ indicates number of cans each has ✓ forms and simplifies equation ✓ correct number

Question 2

(5 marks)

The number of daily absentees at a small school over 15 consecutive days are listed below:

7, 6, 4, 5, 6, 6, 3, 9, 7, 6, 7, 6, 4, 5, 4.

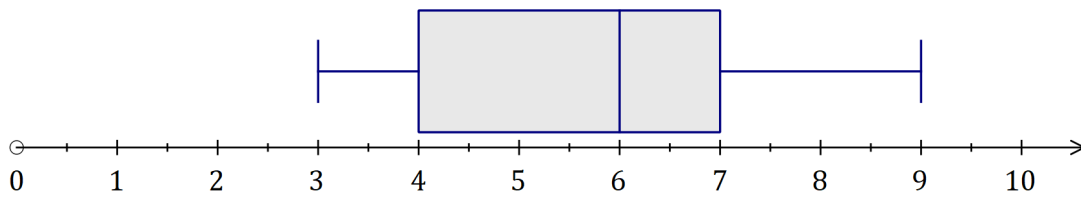
(a) Determine the five-number summary for this data.

(3 marks)

Solution
Ordered: {3, 4, 4}, 4, {5, 5, 6}, 6, {6, 6, 6}, 7, {7, 7, 9}
Median is 6
Q1 is 4, Q3 is 7
Summary is 3, 4, 6, 7 and 9
Specific behaviours
<ul style="list-style-type: none"> ✓ Min and Max ✓ Median ✓ Q1 and Q3

(b) Use the five-number summary to construct a box-plot on the scale below.

(2 marks)

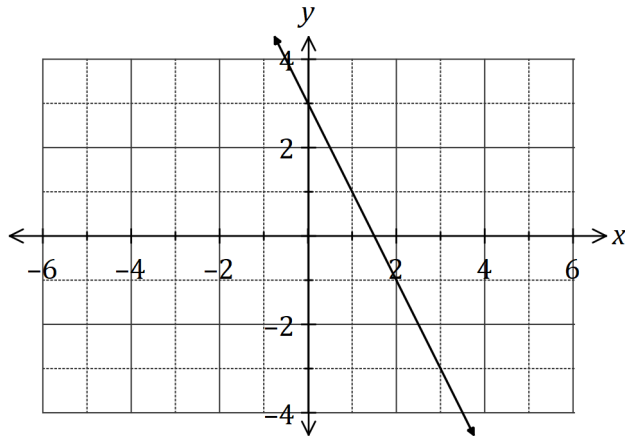


Solution
See graph
Specific behaviours
<ul style="list-style-type: none"> ✓ correctly locates five-number summary points ✓ draws box and whiskers

Question 3

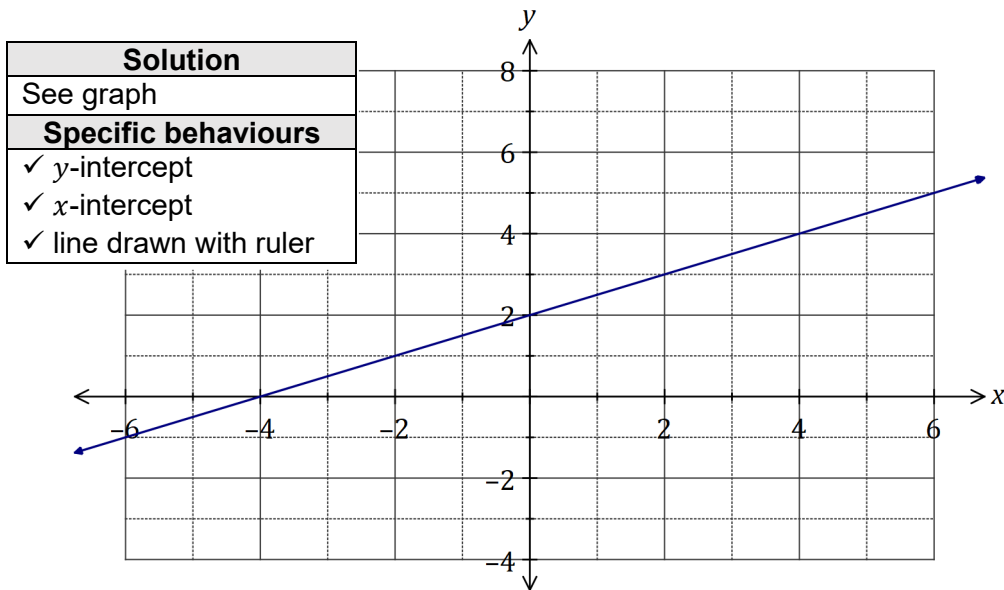
(7 marks)

(a) The graph of $y = ax + b$ is shown below. Determine the values of a and b . (2 marks)



Solution
$a = -2$
$b = 3$
Specific behaviours
<ul style="list-style-type: none"> ✓ correct value for a ✓ correct value for b

(b) Draw the graph of the line $y = \frac{1}{2}x + 2$ on the axes below. (3 marks)



Solution
See graph
Specific behaviours
<ul style="list-style-type: none"> ✓ y-intercept ✓ x-intercept ✓ line drawn with ruler

(c) Determine the gradient of the line $3x - 2y = 12$. (2 marks)

Solution
$2y = 3x - 12$
$y = 1.5x - 6$
Gradient = 1.5
Specific behaviours
<ul style="list-style-type: none"> ✓ rearranges into $y =$ form ✓ states gradient

Question 4

(8 marks)

(a) The power P consumed by a device can be calculated using the formula $P = I^2R + \sqrt{2R}$.

Calculate the value of P when

(i) $I = 5$ and $R = 8$.

(2 marks)

Solution
$P = 5^2 \times 8 + \sqrt{2 \times 8}$
$P = 25 \times 8 + \sqrt{16}$
$P = 200 + 4 = 204$
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes correctly, simplifying I^2 and $2R$ ✓ evaluates correctly

(ii) $I = 0.5$ and $R = 50$.

(2 marks)

Solution
$P = 0.5^2 \times 50 + \sqrt{2 \times 50}$
$P = 0.25 \times 50 + \sqrt{100}$
$P = 12.5 + 10 = 22.5$
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes correctly, simplifying I^2 and $2R$ ✓ evaluates correctly

(b) The variable D is related to diameters d_1, d_2 and d_3 by the formula $D = \frac{d_1}{4} + \frac{2}{d_2 - d_3}$.

Calculate the value of D when

(i) $d_1 = 2, d_2 = 9$ and $d_3 = 1$.

(2 marks)

Solution
$D = \frac{2}{4} + \frac{2}{9-1} = \frac{2}{4} + \frac{2}{8}$
$D = \frac{2}{4} + \frac{1}{4} = \frac{3}{4}$
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes correctly, simplifying $d_2 - d_3$ ✓ evaluates correctly

(ii) $d_1 = 18, d_2 = 3.5$ and $d_3 = 4$.

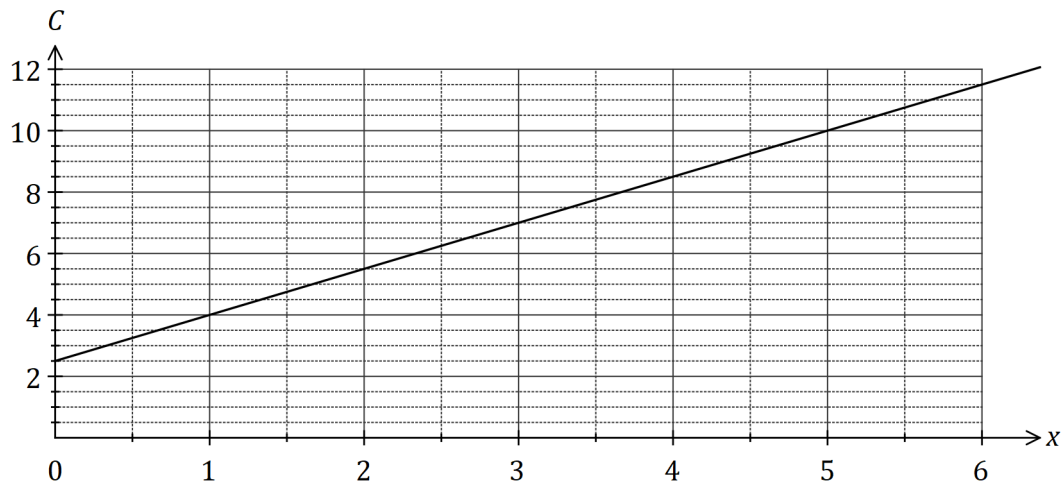
(2 marks)

Solution
$D = \frac{18}{4} + \frac{2}{3.5-4} = \frac{18}{4} + \frac{2}{-0.5}$
$D = 4.5 - 4 = 0.5$
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes correctly, simplifying $d_2 - d_3$ ✓ evaluates correctly

Question 5

(6 marks)

The graph below shows the cost C , in dollars, of taking a journey of x km with a taxi company.



(a) State the cost of taking a 4 km journey.

Solution
\$8.50
Specific behaviours
✓ correct cost

(1 mark)

(b) How much more expensive is a 5 km journey compared to one of 4 km?

Solution
$10 - 8.50 = \$1.50$
Specific behaviours
✓ correct difference

(1 mark)

(c) State and interpret, in context, the value of the vertical axis intercept of the graph.

Solution
\$2.50, a fixed cost payable regardless of distance travelled.
Specific behaviours
✓ value, ✓ interprets as fixed cost, flag-fall, etc

(2 marks)

(d) State and interpret, in context, the value of the gradient of the graph.

Solution
$m = 1.5$, the cost per kilometre of a journey is \$1.50
Specific behaviours
✓ value, ✓ interprets as cost per kilometre

(2 marks)

Question 6

(6 marks)

The heights of 5-year old boys are normally distributed with a mean of 109 cm and a standard deviation of 4 cm.

- (a) Use the 68%, 95%, 99.7% rule to determine the approximate percentage of 5-year old boys that can be expected to have heights between

- (i) 97 and 121 cm.

(2 marks)

Solution
109 ± 12 $\pm 12 \div 4 = \pm 3 \text{ sd's} \Rightarrow 99.7\%$
Specific behaviours
✓ indicates ± 3 sd from mean ✓ correct percent

- (ii) 109 and 113 cm.

(2 marks)

Solution
$113 - 109 = 4$ $4 \div 4 = 1 \text{ sd} \Rightarrow 68 \div 2 = 34\%$
Specific behaviours
✓ indicates 1 sd above mean ✓ correct percent

- (b) Nurses at a health clinic measure the heights of children and refer anyone with a height that is more than two standard deviations from the mean of the child's age group to a doctor.

The last eight boys, aged 5, who attended the clinic had the following heights:

111 108 104 118 112 103 116 109 cm.

Determine, with justification, how many of these boys were referred.

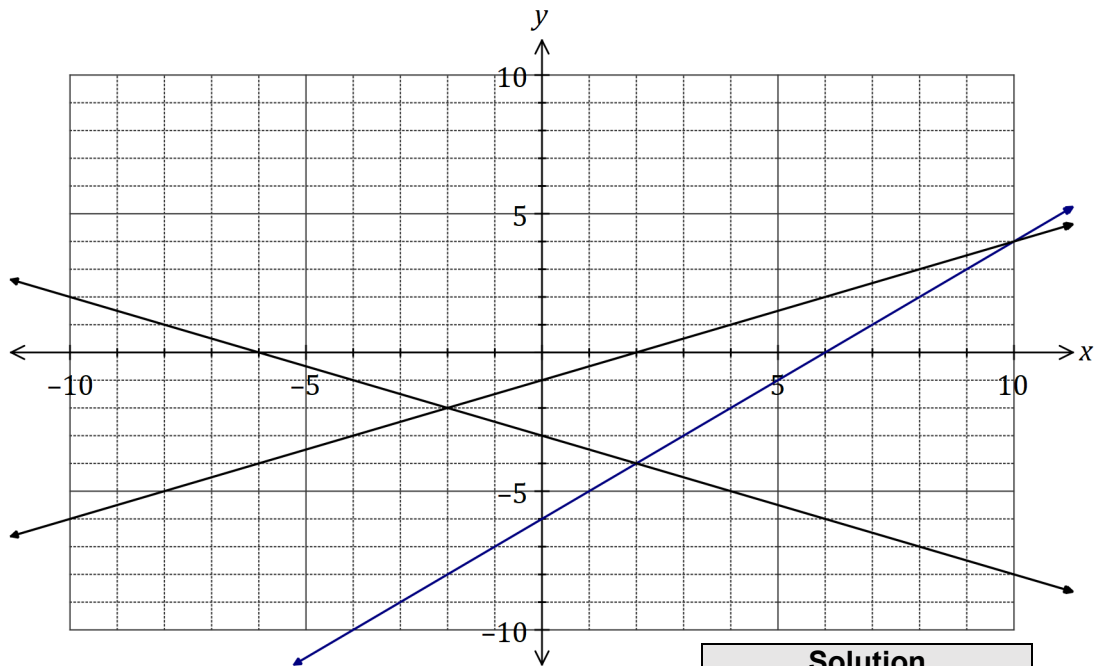
(2 marks)

Solution
Not referred if height between 101 and 117 cm.
So, one boy referred (118 cm).
Specific behaviours
✓ correct number ✓ justification (eg standard score or states bounds)

Question 7

(7 marks)

(a) The lines with equations $2y + 2 = x$ and $2y + x = -6$ are shown on the axes below.



(i) Draw the line $y = x - 6$ on the axes above.

Solution
See graph
Specific behaviours
✓ y-intercept
✓ x-intercept

(2 marks)

(ii) Solve the simultaneous equations $y = x - 6$ and $2y + 2 = x$.

(2 marks)

Solution
From graph, $x = 10, y = 4$
Specific behaviours
✓ indicates appropriate method
✓ correct values of x and y

(b) Solve the simultaneous equations $x + y = 7$ and $2y + x = -6$.

(3 marks)

Solution
$(2y + x = -6)$ $-(x + y = 7)$ $y = -13$ $x - 13 = 7$ $x = 20$
Specific behaviours
✓ indicates use of substitution or elimination
✓ solves for y
✓ solves for x

Question 8

(8 marks)

A group of friends who frequently travelled abroad exchanged foreign currency between themselves using the conversion table below. For example, members of the group could exchange 100 dollars for 20 dinars or 50 kroner for 10 dollars.

Country/Currency	Australian/Dollar			
	10	20	50	100
Denmark/Krone	50	100	250	500
Japan/Yen	800	1 600	4 000	8 000
Kuwait/Dinar	2	4	10	20
Thailand/Baht	250	500	1 250	2 500

- (a) How many baht can be exchanged for 30 dollars? (1 mark)

Solution
$\$30 = \$20 + \$10 = 500 + 250 = 750$ baht
Specific behaviours
✓ correct amount

- (b) How many dollars can be exchanged for 20 000 yen? (2 marks)

Solution
$20000 = 8000 + 8000 + 4000$ $= 100 + 100 + 50$ $= 250$ dollars
Specific behaviours
✓ appropriate method ✓ correct amount

- (c) Before travelling to Kuwait, one of the group exchanged 490 dollars for the local currency. How many dinars did they receive? (2 marks)

Solution
$490 = 5 \times 100 - 10$ $= 5 \times 20 - 2$ $= 98$ dinars
Specific behaviours
✓ appropriate method ✓ correct amount

- (d) Another member of the group exchanged 500 dollars for a mixture of 1 350 kroner and some yen. Determine the amount of Japanese currency they received. (3 marks)

Solution
$1350 = 500 + 500 + 250 + 100$ $= \$100 + \$100 + \$50 + \20 $= \$270$
$\$500 - \$270 = \$230$
$\$230 = \$100 + \$100 + \$20 + \$10$ $= 8000 + 8000 + 1600 + 800$ $= 18\,400$ yen
Specific behaviours
✓ converts kroner to dollars ✓ calculates remaining dollars ✓ converts dollars to yen

End of questions



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**MATHEMATICS
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UNITS 1 AND 2
Section Two:
Calculator-assumed**

SOLUTIONS

Student number: In figures

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In words

Your name

Time allowed for this section

Reading time before commencing work: ten minutes
Working time: one hundred minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet
Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Section Two: Calculator-assumed

65% (98 Marks)

This section has **thirteen (13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9

(5 marks)

The following matrix S shows the number of small sheds (in row 1) and large sheds (in row 2) sold by a company in each of three consecutive months. For example, the element S_{13} represents the number of small sheds sold during the third month.

$$S = \begin{bmatrix} 72 & 68 & 75 \\ 51 & 59 & 38 \end{bmatrix}$$

- (a) How many large sheds were sold in the second month? (1 mark)

Solution
59 sheds
Specific behaviours
✓ correct number

- (b) Calculate matrix A , where $A = S \times \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$. (1 mark)

Solution
$A = \begin{bmatrix} 215 \\ 148 \end{bmatrix}$
Specific behaviours
✓ correct matrix

- (c) Explain what information matrix A shows. (1 mark)

Solution
Number of small and large sheds sold over the 3-month period.
Specific behaviours
✓ clear explanation

Matrix $P = [141 \quad 236]$, where P_{11} and P_{12} represent the profit, in dollars, made by selling a small shed and a large shed respectively.

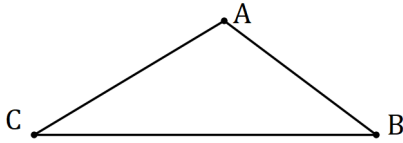
- (d) Using matrices A and P , write down a calculation that will result in a matrix showing the total profit from selling all the sheds over the three-month period and state this profit. (2 marks)

Solution
$[141 \quad 236] \times \begin{bmatrix} 215 \\ 148 \end{bmatrix} = [65243]$
Profit is \$65 243
Specific behaviours
✓ product shown in correct order
✓ correct profit

Question 10

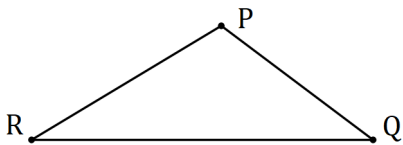
(5 marks)

- (a) Show use of trigonometry to determine the length of side BC in the triangle below, where $\angle BAC = 122^\circ$, $AB = 58$ cm and $AC = 71$ cm. (2 marks)



Solution
$BC^2 = 58^2 + 71^2 - 2(58)(71) \cos 122$
$BC = 113$ cm
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes correctly into cosine rule ✓ correct length

- (b) Show use of trigonometry to determine the size of angle $\angle PRQ$ in the triangle below, where $\angle QPR = 105^\circ$, $PR = 45$ cm and $QR = 65$ cm. (3 marks)

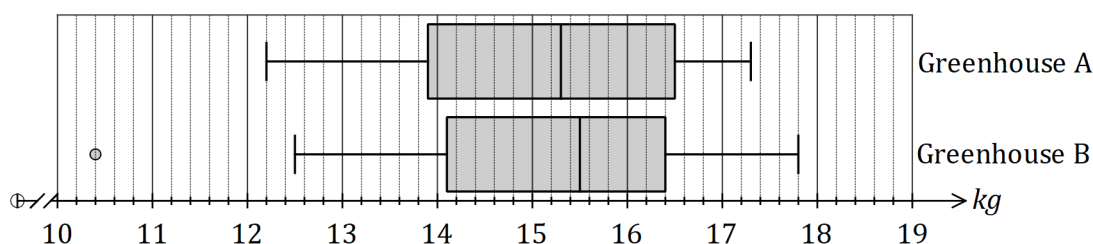


Solution
If $x = \angle PQR$ then $\frac{\sin x}{45} = \frac{\sin 105}{65}$
$x = 42^\circ$
$\angle PQR = 180 - 105 - 42 = 33^\circ$
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes correctly into sine rule ✓ correct value for $\angle PRQ$ ✓ size of required angle

Question 11

(8 marks)

A hydroponic grower was trialling two different greenhouse systems for growing tomatoes. To compare the systems, the weight of tomatoes produced by each plant in the two greenhouses were recorded. The data is summarised below.



- (a) Ignoring the outlier, compare the range of weights produced by plants in greenhouse A with that of greenhouse B. (2 marks)

Solution
$A: 17.3 - 12.2 = 5.1, \quad B: 17.8 - 12.5 = 5.3$ The range of A is smaller than that of B.
Specific behaviours
✓ indicates both ranges ✓ comparison of ranges

- (b) State and use the interquartile ranges to compare the spread of weights produced by plants in greenhouse A with that of greenhouse B. (2 marks)

Solution
$A: 16.5 - 13.9 = 2.6, \quad B: 16.4 - 14.1 = 2.3$ The spread of weights in A is larger than the spread of weights in B.
Specific behaviours
✓ indicates both IQRs ✓ comparison of spreads

- (c) Using the result of a relevant calculation, explain why one of the weights in greenhouse B was identified as an outlier. (2 marks)

Solution
$14.1 - 1.5 \times 2.3 = 10.65$ The weight of 10.4 is an outlier as it is below 10.65.
Specific behaviours
✓ calculates $LQ - 1.5 \times IQR$ ✓ states weight of outlier and that it is below cut-off

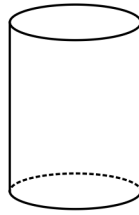
- (d) Explain whether there is evidence to support the conjecture that the system in one greenhouse produces a larger crop of tomatoes than the other. (2 marks)

Solution
Yes, since the median weight from B exceeds that from A and the plant producing the largest crop was in greenhouse B.
Specific behaviours
✓ states there is evidence ✓ valid explanation

Question 12

(7 marks)

Soup is sold in cylindrical tins that have an internal diameter of 7.6 cm and a height of 13.6 cm.



- (a) Calculate the internal surface area of the can.

(3 marks)

Solution
$r = 7.6 \div 2 = 3.8$
$A = 2\pi \times 3.8^2 + 2\pi \times 13.6$ $= 415 \text{ cm}^2$
Specific behaviours
<ul style="list-style-type: none"> ✓ indicates correct radius ✓ substitutes into formula ✓ evaluates

- (b) Calculate the capacity of the can in millilitres. (1 mL = 1 cm³)

(2 marks)

Solution
$V = \pi \times 3.8^2 \times 13.6$ $= 617 \text{ mL}$
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes into formula ✓ evaluates

- (c) Before the cans are sealed, they are stood on their circular end and filled with 540 mL of soup. Determine the depth of soup in the can.

(2 marks)

Solution
$540 = \pi \times 3.8^2 \times h$ $h = 11.9 \text{ cm}$
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes into formula ✓ solves for h

Question 13

(7 marks)

Individual use coffee bags are packed in boxes of 8, 18 or 28. Customers can buy cartons containing 4, 5 or 6 boxes, as shown in the following table.

Carton	Carton price (\$)	Boxes per carton	Coffee bags per box
A	39.20	4	28
B	17.76	6	8
C	30.60	5	18

- (a) A customer orders a total of 16 cartons, comprising 7 of type A, 4 of type B and the rest of type C. Calculate the cost of this order, given that orders of more than \$150 qualify for a 25% discount. (3 marks)

Solution
$7 \times 39.20 = 274.40$ $4 \times 17.76 = 71.04$ $5 \times 30.60 = 153.00$ Total = 498.44 $498.44 \times 0.75 = \$373.83$
Specific behaviours
✓ cost of A's and B's ✓ cost of C's and total cost ✓ correct cost with discount

- (b) Determine the cost of one coffee bag in each type of carton and hence list the carton types from best to worst value in terms of the price per coffee bag. (4 marks)

Solution
A: $4 \times 28 = 112$ $39.20 \div 112 = \$0.35$ B: $6 \times 8 = 48, 17.76 \div 48 = \0.37 C: $5 \times 18 = 90, 30.60 \div 90 = \0.34 Best to worst: C, A, B
Specific behaviours
✓ calculates number of bags in a carton ✓ calculates unit cost for same carton ✓ calculates all unit costs ✓ correct ranking (based on seen unit costs)

Question 14

(11 marks)

As part of an investigation into youth fitness, a researcher collected the sit-and-reach (SR) measurements of 250 students. The data is summarised in the table below.

SR measurement (cm)	Number of students
$18 < x \leq 22$	5
$22 < x \leq 26$	10
$26 < x \leq 30$	32
$30 < x \leq 34$	68
$34 < x \leq 38$	90
$38 < x \leq 42$	36
$42 < x \leq 46$	9

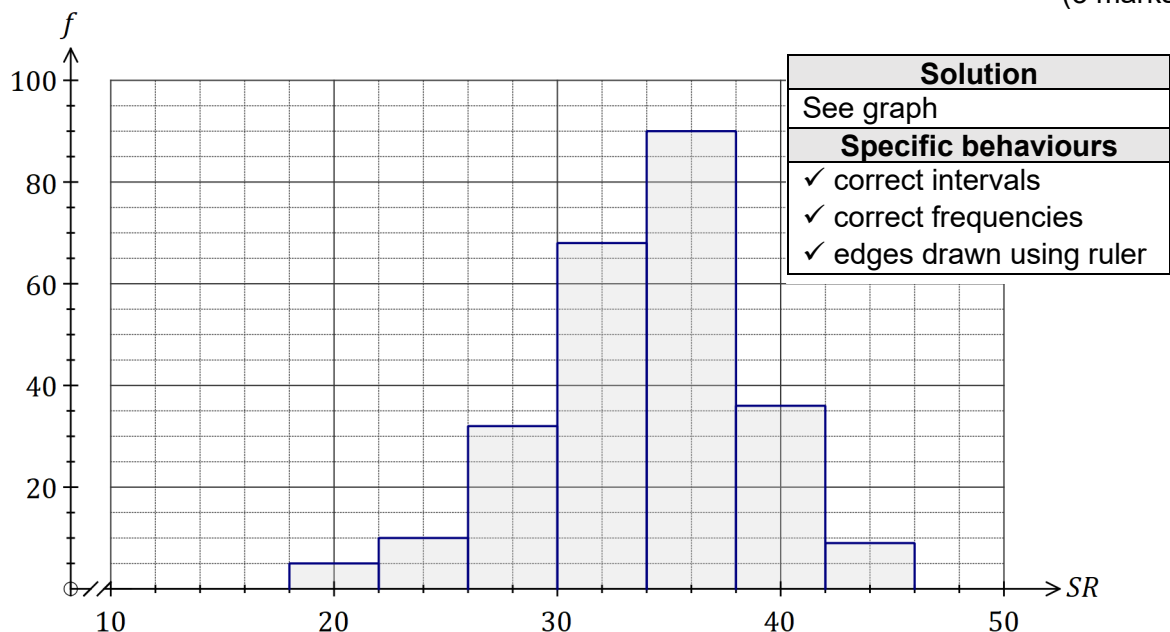
- (a) Use the mid-point of each class interval to determine the mean and standard deviation of the sit-and-reach measurements. (2 marks)

Solution
$\bar{x} = 33.95 \text{ cm}, \quad sd = 4.88 \text{ cm}$
Specific behaviours
<ul style="list-style-type: none"> ✓ correct mean ✓ correct sd

- (b) Explain why it was necessary to use the mid-point of each class interval to determine the statistics in (a). (1 mark)

Solution
Data has been grouped; No access to raw data; Best estimate for students in each interval; etc, etc
Specific behaviours
✓ any reasonable explanation

- (c) Draw a histogram on the axes below to display the distribution of SR measurements. (3 marks)



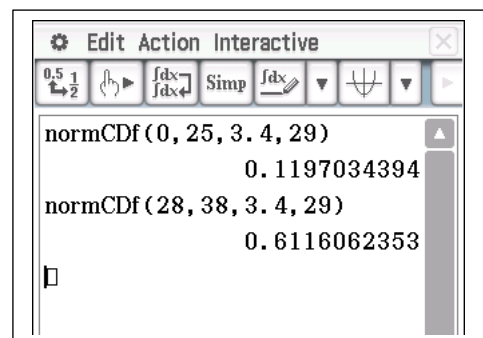
- (d) Use features of the histogram to describe the distribution of SR measurements for this group of students. (3 marks)

Solution
-The dataset is negatively skewed (skewed left). -The dataset is unimodal, with 34 – 38 the modal group. -The bulk of measurements lie between 26 and 42 cm, with just a handful outside this interval. -The frequencies increase up to the modal group and then decrease. -There is no indication of any outliers. -Etc etc
Specific behaviours
✓ describes shape ✓ describes modality ✓ describes one other feature

- (e) In a previous investigation, the researcher found that the SR measurements for an older group of people were normally distributed with a mean of 29 cm and a standard deviation of 3.4 cm. Determine the percentage of people in this older group who had an SR measurement

- (i) less than 25 cm. (1 mark)

Solution
$P(X < 25) = 12\%$
Specific behaviours
✓ correct percentage



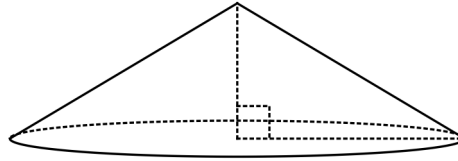
- (ii) between 28 and 38 cm. (1 mark)

Solution
$P(28 < X < 38) = 61\%$
Specific behaviours
✓ correct percentage

Question 15

(8 marks)

The roof of a circular building has the shape of a right-circular cone with a base radius of 5.6 m and a perpendicular height of 3.3 m.



- (a) Building regulations require that one air vent is required for every 30 m^3 of space (or part) in the roof. Determine the number of air vents required for the roof shown. (3 marks)

Solution
$V = (\pi \times 5.6^2 \times 3.3) \div 3$ $= 108.4 \text{ m}^3$
$108.4 \div 30 = 3.6$ Need 4 air vents
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes correctly ✓ correct volume ✓ states required number of air vents

- (b) The curved surface of the roof is to be tiled (excluding the circular base). The tile that the builder has chosen has a coverage rate of 16 tiles per square metre and can be bought in packs of 124. Determine the number of packs the builder must order. (5 marks)

Solution
$s = \sqrt{5.6^2 + 3.3^2} = 6.5 \text{ m}$
$A = \pi \times 5.6 \times 6.5$ $= 114.4 \text{ m}^2$
Tiles = $114.4 \times 16 = 1830$
Packs = $1830 \div 124 = 14.7$ Order 15 packs
Specific behaviours
<ul style="list-style-type: none"> ✓ calculates slant height ✓ uses formula for curved surface area ✓ calculates surface area ✓ calculates number of tiles ✓ calculates number of packs

Question 16

(8 marks)

(a) The statistical investigation process is a cyclical process that begins with the need to solve a real-world problem and aims to reflect the way statisticians work. Step *P* is one of the four steps in the cyclical process and involves the design and implementation of a plan to collect or obtain appropriate data.

(i) Describe the key elements of the step immediately after *P* in the cyclical process. (2 marks)

Solution
Select and apply appropriate graphical or numerical techniques to analyse the data.
Specific behaviours
✓ indicates analysis ✓ indicates use of graph or calculation

(ii) Describe the key elements of the step immediately before *P* in the cyclical process. (2 marks)

Solution
Clarify the problem and formulate one or more questions that can be answered with data.
Specific behaviours
✓ indicates clarify/identify problem ✓ indicates formulation of question(s)

(b) A student was carrying out a statistical investigation involving dogs.

(i) Describe an example of a categorical variable the student could investigate and list two different responses that could be recorded. (2 marks)

Solution
Type of breed: Poodle, terrier Type of coat: Silky, wiry Etc etc.
Specific behaviours
✓ valid example relating to dogs ✓ two different and valid responses

(ii) Describe an example of a continuous numerical variable the student could investigate and list two different responses that could be recorded. (2 marks)

Solution
Weight: 8.5 kg, 7.2 kg Length of tail: 5 cm, 56 cm. Etc etc.
Specific behaviours
✓ valid example relating to dogs ✓ two different and valid responses with units

Question 17

(9 marks)

A second-hand car yard paid \$33 500 for a vehicle and later sold it to a customer for \$26 930.

(a) Calculate the percentage loss made on the sale.

(2 marks)

Solution
$33500 - 26930 = 6570$
$\frac{6570}{33500} \times 100 = 19.6\% \text{ loss}$
Specific behaviours
<ul style="list-style-type: none"> ✓ calculates loss ✓ correct percentage

(b) The customer paid a deposit of \$2 930 and took out a loan for the remainder of the price with an interest rate of 10.9% per annum. Calculate the simple interest on the loan for the first month. (3 marks)

Solution
$26930 - 2930 = 24000$
$24000 \times 0.109 = 2616$
$2616 \div 12 = \$218$
Specific behaviours
<ul style="list-style-type: none"> ✓ calculates principle ✓ interest for one year ✓ interest for one month

(c) The price the customer paid included 10% GST. Calculate the amount of GST included in the price. (2 marks)

Solution
$\frac{26930}{11} = \$2\,448.18$
Specific behaviours
<ul style="list-style-type: none"> ✓ correct method ✓ amount of GST

(d) The standard premium to insure the vehicle was \$2 388, but the customer was offered a discount of 35% for not having made any claims over the past five years. Determine the premium after the discount was applied. (2 marks)

Solution
$2388 \times 0.65 = \$1\,552.20$
Specific behaviours
<ul style="list-style-type: none"> ✓ correct method ✓ correct premium

Question 18

(8 marks)

The top of a vertical pole T stands 6.4 m above a surrounding level playing field. The angle of depression from T to a small animal at A is 32° . The animal leaves A , moves directly towards the base of the pole B and stops at C (before reaching B). The distance BC is 5.5 m.

(a) Sketch a diagram to show the above information.

(2 marks)

Solution
Specific behaviours
<ul style="list-style-type: none"> ✓ vertical TB with angle of depression to A ✓ lengths TB and BC, making a right-angle

(b) Calculate the line of sight distance from the top of the pole to A .

(2 marks)

Solution
$AT = 6.4 \div \sin 32$ $= 12.1 \text{ m}$
Specific behaviours
<ul style="list-style-type: none"> ✓ uses sine ratio ✓ correct distance

(c) Determine the angle of depression from T to C .

(2 marks)

Solution
$\angle TCB = \tan^{-1} \frac{6.4}{5.5}$ $= 49.3^\circ$
Specific behaviours
<ul style="list-style-type: none"> ✓ uses tangent ratio ✓ correct angle (to nearest degree)

(d) Calculate the distance travelled by the animal from A to C .

(2 marks)

Solution
$AB = 6.4 \div \tan 32 = 10.2 \text{ m}$
$AC = 10.2 - 5.5 = 4.7 \text{ m}$
Specific behaviours
<ul style="list-style-type: none"> ✓ calculates AB ✓ calculates AC

Question 19

(7 marks)

The wind chill index I is a measure of how quickly a person exposed to a wind will lose heat. It is calculated using the formula below, where v is the speed of the wind in metres per second and T is the air temperature in degrees Celsius.

$$I = (10\sqrt{v} - v + 10.2)(34 - T)$$

- (a) Determine I when the air temperature is -3°C and there is a wind of 12 m/s blowing.

(2 marks)

Solution
$I = (10\sqrt{12} - 12 + 10.2)(34 - -3)$ $= 1215$
Specific behaviours
<ul style="list-style-type: none"> ✓ correct substitution ✓ evaluates

- (b) Calculate the change in the wind chill index when the air temperature is -8°C and the strength of the wind decreases from 22 m/s to 8 m/s.

(3 marks)

Solution
$I = (10\sqrt{22} - 22 + 10.2)(34 - -8)$ $= 1474$
$I = (10\sqrt{8} - 8 + 10.2)(34 - -8)$ $= 1280$
$\text{Decrease} = 1474 - 1280 = 194$
Specific behaviours
<ul style="list-style-type: none"> ✓ first value correct ✓ second value correct ✓ indicates decrease and states amount

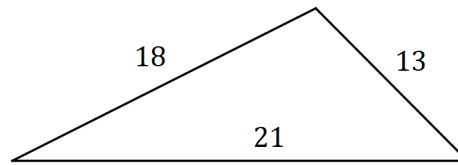
- (c) A person is likely to suffer from frostbite when the wind chill index reaches 1 500. At what temperature will this happen, on a day when the wind has a speed of 25 m/s? (2 marks)

Solution
$1500 = (10\sqrt{25} - 25 + 10.2)(34 - T)$ $1500 = 35.2(34 - T)$
$T = 34 - \frac{1500}{35.2}$ $= -8.6^\circ\text{C}$
Specific behaviours
<ul style="list-style-type: none"> ✓ substitutes and simplifies ✓ solves for temperature

Question 20

(7 marks)

A model of a triangular gable has measurements shown below, in centimetres.



- (a) Use Heron's rule to determine the area of the model of the gable.

(3 marks)

Solution
$s = \frac{18 + 13 + 21}{2} = 26$
$A = \sqrt{26(26 - 18)(26 - 13)(26 - 21)}$ $= 116.3 \text{ cm}^2$
Specific behaviours
<ul style="list-style-type: none"> ✓ calculates semi-perimeter ✓ substitutes into Heron's rule ✓ correct area

The model was drawn to a scale using measurements taken from a building, where the length of the shortest side of the gable was 5.2 m.

- (b) Calculate the scale factor used to draw the model.

(1 mark)

Solution
$5.2 \times \frac{100}{13} = 40 \Rightarrow \text{SF} = 1:40$
Specific behaviours
<ul style="list-style-type: none"> ✓ correct scale factor

- (c) The gable on the building requires repainting, at a cost of \$21 per square metre. Determine the cost of repainting the gable, to the nearest dollar.

(3 marks)

Solution
$\text{Area} = 116.3 \times (40 \div 100)^2$ $= 116.3 \times 0.16$ $= 18.6 \text{ m}^2$
$\text{Cost} = 18.6 \times 21 \approx \391
Specific behaviours
<ul style="list-style-type: none"> ✓ indicates area scale factor ✓ building area ✓ calculates cost, rounding

Question 21

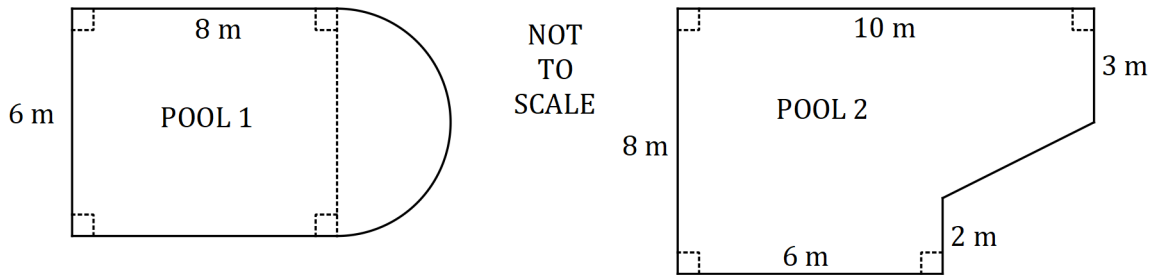
(8 marks)

When working out the cost of building an in-ground swimming pool, a contractor calculates a shape factor k to use in a spreadsheet, where

$$k = \frac{P^2}{4A}$$

P is the perimeter of the pool in metres and A is the area of the pool in square metres.

Pool 1 is rectangular with a semi-circular end and pool 2 is rectangular with a cut-out as shown.



Determine, with justification, which of the pools shown has the larger shape factor k .

Solution	
Pool 1	$A_1 = 6 \times 8 + \frac{1}{2} \times \pi \times 3^2 = 62.14$ $P_1 = 8 + 6 + 8 + \frac{1}{2} \times 2 \times \pi \times 3 = 31.42$ $k_1 = \frac{31.42^2}{4 \times 62.14} = 3.97$
Pool 2	$A_2 = 8 \times 10 - 2 \times 4 - \frac{1}{2} \times 4 \times 3 = 66$ $P_2 = 3 + 10 + 8 + 6 + 2 + x = 29 + x$ $x = \sqrt{4^2 + 3^2} = 5$ $P_2 = 34$ $k_2 = \frac{34^2}{4 \times 66} = 4.38$
Pool 2 has the larger shape factor.	
Specific behaviours	
<ul style="list-style-type: none"> ✓ area of pool 1 ✓ perimeter of pool 1 ✓ k for pool 1 ✓ area of pool 2 ✓ indicates missing length in pool 2 ✓ perimeter of pool 2 ✓ k for pool 2 ✓ identifies pool with larger k 	